Applied Photonics in Metamaterials

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Motivation for Metamaterials

- Diffraction Limit hurdle to higher resolution
- Localized Surface Plasmons: EM fields generated by resonant oscillations of electron plasma in metals
- Manipulating light at the subwavelength scale with new class of materials – "Metamaterials"

Index

- Plasmonics: origin, importance and applications
- Enhanced Transmission through Subwavelength hole
- Localized Plasmon Resonances in Metal Nanoparticles
- Metamaterials: Specific Applications
- Summary: Important results

Plasmonics: Origin

- Nanotechnology: Scaling down of devices
- Moore's law for electronics- doubling of components per unit area in transistors but no corresponding observation for optical devices
- Electronic component size has reduced to ten nanometers but optical components are still at hundreds of nanometers
- Plasmonics gained significant attention and research input because it provided the possibility to scale down optical components to subwavelength scales

What is stopping miniaturization of optical devices?

- Diffraction limit
- 3D conventional devices limiting planar integration
- Sharp corners being very lossy for electromagnetic fields in optical components

Plasmonics: Origin

- Limitation of optical imaging discovered by Abbe [1] and Rayleigh [2] due to the diffraction limit
- Ebbesen's [3] discovery of extraordinary transmission
- Study of electromagnetic properties of metal-dielectric interface by Mie and Ritchie revealed that these interfaces can sustain coherent electron oscillations called surface plasmon polaritons (SPPs) leading to EM fields confined to the metallic surface

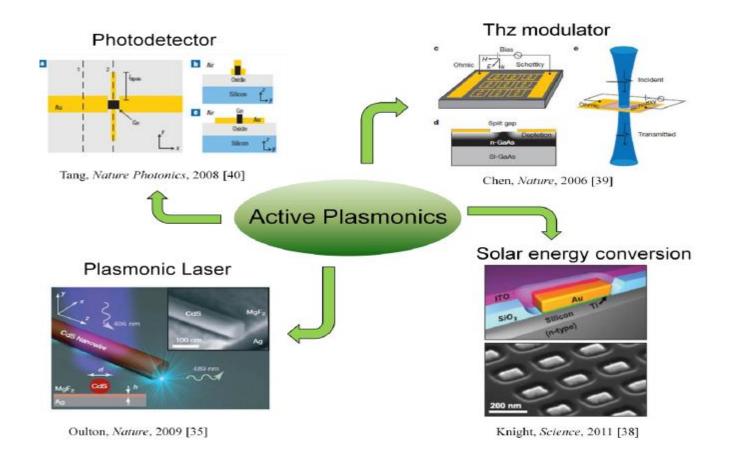
Plasmonics: Importance and Applications

- SPPs have wavelength shorter than that of light propagating in free space making on-chip subwavelength optics possible as in electrical devices
- This has found application in surfaced enhanced Raman spectroscopy, electron beam lithography, ion beam milling and near field microscopy
- New generation of materials termed "plasmonic metamaterials" emerged [4]
- Novel optical properties- negative index of refraction have been proposed and demonstrated [5,6,7]

Plasmonics: Importance and Applications

- Exotic optical devices- the invisibility cloak have been realized [8, 9]
- Light generated from a plasmonic cavity displays the Purcell effect which is used to make nanoscale laser demonstrated by several groups [10, 11, 12, 13]
- A strong localized field improves solar energy harvesting in the offbandgap near-IR region [14]
- The THz optical modulator based on split ring resonator (SRR), has been demonstrated [15]
- A nanoscale plasmonic dipole antenna used to improve the efficiency of the photodetector at a near-IR range [16]

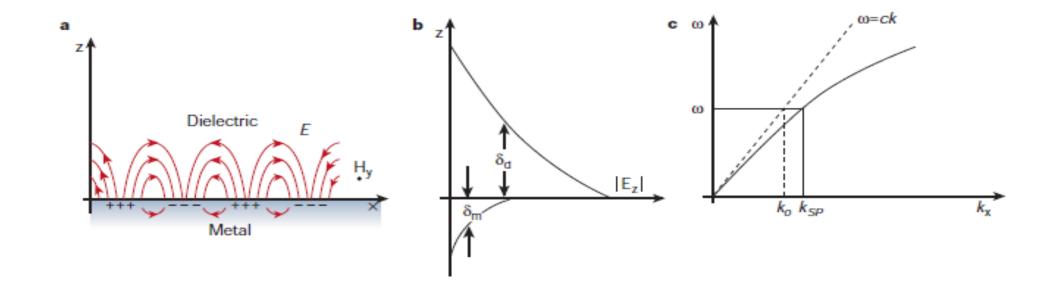
Plasmonics: Applications



Plasmons

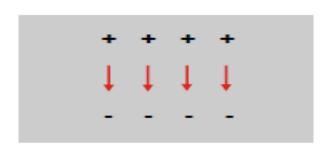
- The word plasmons comes from plasma oscillations
- Electron plasma oscillations in metal form plasmons
- Plasmons in bulk oscillate at ω_p (plasma frequency)
- Resonant surface plasmon polariton (SPP) modes are formed on the surface of metal dielectric interface
- Localized surface plasmon resonance modes are supported in spherical metal nanoparticles

SPP on Metal Dielectric interface



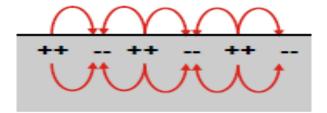
Plasma oscillations in various geometries

Bulk metal



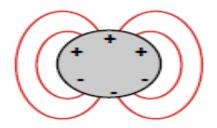
$$\omega_p$$
 $\varepsilon = 0$

Metal surface



$$\varepsilon = -1$$
 $\xrightarrow{\text{drude}}$ $\omega_p / \sqrt{2}$ model

Metal sphere localized SPPs



$$\varepsilon = -2 \qquad \xrightarrow[\text{model}]{} \qquad \omega_p \left/ \sqrt{3} \right.$$

Enhanced Transmission through Subwavelength Hole

- Theory of Diffraction: Kirchhoff
- Bethe's Analytical Solution
- Extraordinary Transmission

Theory of Diffraction

- Kirchhoff [17] attempted to explain Huygens-Fresnel principle.
- His theory worked fairly well in optical region where size of structure is lesser than wavelength.
- It failed due to assumption of scalar formulation which is contradicted by solution of the Helmholtz equation for given boundary conditions.

- Helmholtz Equation $\nabla^2 u + k^2 u = 0$
- Boundary Condition on the screen

$$u_{screen} = 0$$
 , $\frac{\partial u_{screen}}{\partial x'} = 0$

Using Green's Theorem with

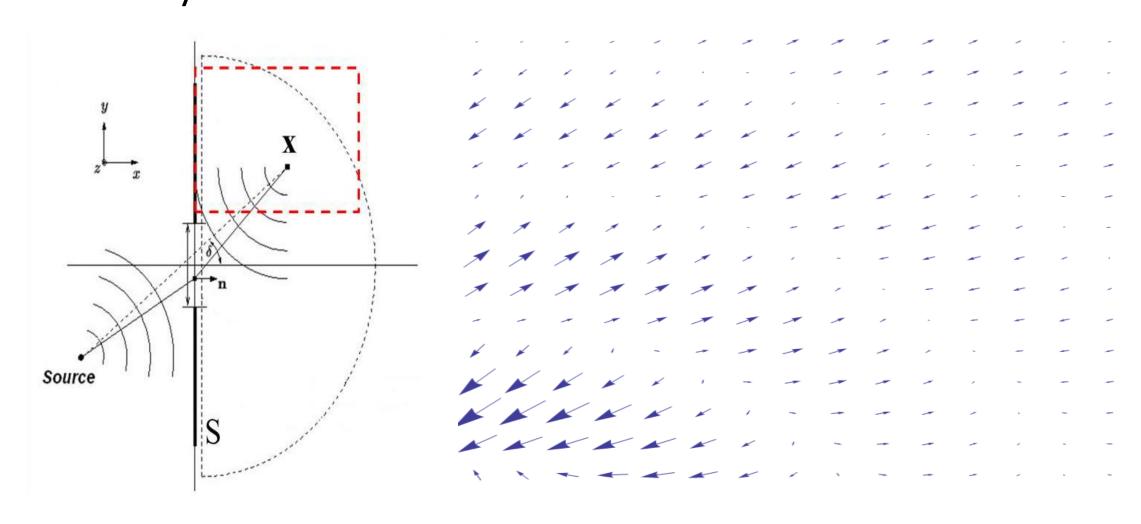
$$G(\mathbf{x}, \mathbf{x}') = \varphi(|\mathbf{x} - \mathbf{x}'|) = \varphi(r) = e^{ikr} / r \text{, we get } u(\mathbf{x}) = \int_{S} da \left[-\frac{\partial u_0}{\partial x'} (\mathbf{x}') \varphi(|\mathbf{x} - \mathbf{x}'|) + u_0(\mathbf{x}') \frac{\partial \varphi}{\partial x'} \right]$$

Assuming uniform field over small hole

$$u(r) = -A \left[\frac{\partial u_0}{\partial x'} \varphi(r) + u_0 \frac{\partial \varphi(r)}{\partial x} \right]$$

 On the screen outside hole area, second term vanishes but first term does not giving contradiction to initial assumption

Vector Extensions of Kirchhoff's Diffraction Theory



Bethe's Analytical solution

 In terms of magnetic charge and current, Maxwell's equation can be written as follows

$$\nabla \cdot E = 0, \nabla \times E + \frac{1}{c} \frac{\partial \rho^*}{\partial t} = -4\pi J^*, \ \nabla \cdot H = 4\pi \rho^*, \nabla \times H = \frac{1}{c} \frac{\partial E}{\partial t}$$

- It is well known in electrostatics that a uniform dipole density gives uniform field distribution in the spheroid
- Approximating for a very thin oblate spheroid surface, solving for boundary conditions yield total magnetic charge and current densities

$$\eta = -\frac{\mathbf{x'} \cdot H_0}{\pi \sqrt{a^2 - \mathbf{x'}^2}} \ , \ K = K_m + K_E = \frac{1}{\pi^2} \left(ik \sqrt{a^2 - \mathbf{x'}^2} H_0 + \frac{\mathbf{x'} \times E_0}{2\sqrt{a^2 - \mathbf{x'}^2}} \right)$$

Bethe's Analytical solution

 The field distribution of the diffracted wave can be directly calculated from given charge and current density:

$$E(\mathbf{x}) = \int K(\mathbf{x}') \times \nabla \varphi d\sigma = \frac{1}{3\pi} k^2 a^3 \varphi_0 \kappa \times (2H_0 + E_0 \times \kappa),$$

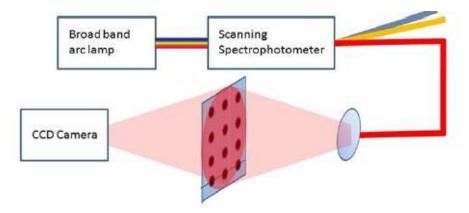
$$H(\mathbf{x}) = \int (ikK(\mathbf{x}')\varphi - \eta(\mathbf{x}')\nabla\varphi)d\sigma = -\frac{1}{3\pi}k^2a^3\varphi_0\kappa \times (2H_0 \times \kappa - E_0)$$

 This field distribution is exactly same as essentially, in-plane magnetic dipole and normal electric dipole are generated in the hole, which satisfy the boundary conditions. Total cross section of a single hole is calculated by integration of the Poynting vector:

$$S_{tot} = \frac{c}{27\pi^2} k^4 a^6 (4H_0^2 + E_0^2) \qquad T = \frac{64}{27\pi^2} k^4 r^4$$

Extraordinary transmission

- T.W. Ebbesen first reported experimental observation of transmission through subwavelength holes at optical region in 1998
- The transmission was found to be three orders of magnitude greater than expected by Bethe's theory
- There were strong transmission peaks when the periodicity of the array matched that required to excite surface plasmon polaritons (SPPs), implying SPPs play significant role in transmission



Localized Plasmon Resonances in Metal Nanoparticles

- Spherical Metal Nanoparticles
- Mie Theory
 - Drude Lorentz Model of metals
- Light scattering off small spheres

Spherical Metal Nanoparticles

- The first theoretical study of small sphere scattering of light was done in Gustav Mie's seminal 1908 paper *Beiträge zur Optik trüber Medien, speziell kolloidaler Metallösungen* (contributions to the optics of turbid media, particularly solution of colloidal metals).
- In 1970, Uwe Kreibig and Peter Zacharias performed a study in which they compared the electronic and optical response of gold and silver nanoparticles. In their work, for the first time they describe the optical properties of metal nanoparticles in terms of surface plasmons.

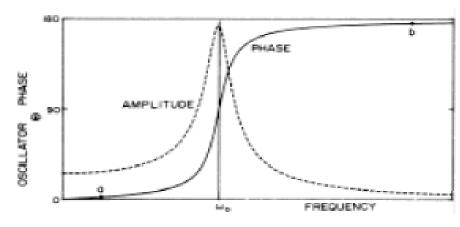
Mie Theory Drude Lorentz Model of metals

• Lorentz model of electrons as damped oscillator giventz equations of motion:

$$m\ddot{x} + b\dot{x} + Kx = eE$$
$$\ddot{x} + \gamma\dot{x} + \omega_0^2 x = \frac{e}{m}E$$

Fourier transform to give solution:

$$x = \frac{(e/m)E}{\omega_0^2 - \omega^2 - i\gamma\omega}$$



Drude

Drude Lorentz Model of metals

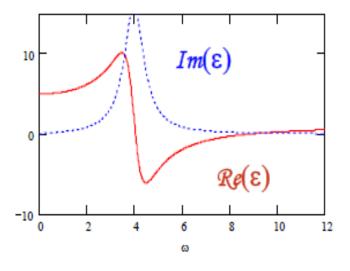
Polarization = (N/V)ex

$$P = \frac{\omega_p^2 \varepsilon_0 E}{\omega_0^2 - \omega^2 - i\gamma\omega}$$

• P = $\chi \epsilon_0 E$ defines χ , and therefore also the dielectric $\epsilon = 1 + \chi$

$$Re\{\varepsilon\} = 1 + \frac{\omega_p^2(\omega_0^2 - \omega^2)}{(\omega_0^2 - \omega^2)^2 + \gamma^2 \omega^2}$$

$$Im\{\varepsilon\} = \frac{\omega_p^2(\omega_0^2 - \omega^2)}{(\omega_0^2 - \omega^2)^2 + \gamma^2 \omega^2}$$



Drude Lorentz Model of metals

• Drude model free electrons hence no ω_0 je. ω_0 =0

$$Re\{\varepsilon\} = 1 - \frac{\omega_p^2}{\omega_p^2 + \gamma^2}$$

$$Im\{\varepsilon\} = \frac{\omega_p^2 \gamma}{\omega(\omega^2 + \gamma^2)}$$

• For $\omega >> \Upsilon$,

$$Re\{\varepsilon\} = 1 + \frac{\omega_p^2}{\omega^2}$$
$$Im\{\varepsilon\} = \frac{\omega_p^2 \gamma}{\omega^3}$$

Drude Lorentz Model of metals

• Susceptibilities (χ) are additive, so can describe real metals with both free and bound charges as

$$\varepsilon = 1 + \chi_{Drude} + \sum_{0}^{n} \chi_{Lorentz}$$

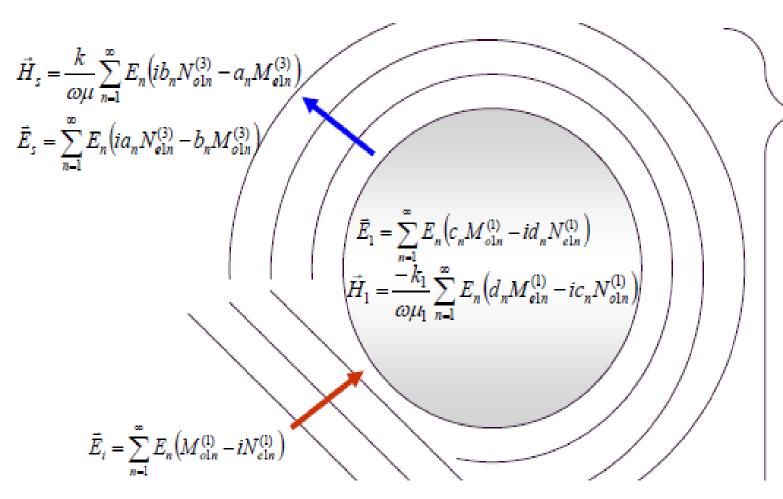
Light scattering off small spheres

• Write field as a superposition of M, N weighted by coefficients an and bn. Here subscript "n" indicates degree of Bessel function.

$$\vec{E}_s = \sum_{n=1}^{\infty} E_n \left(i a_n N_{e1n}^{(3)} - b_n M_{o1n}^{(3)} \right)$$

- Internal field: the j Bessel functions, finite at the origin
- Scattered field: the h(1) Hankel functions, outgoing waves at infinity
- Incident field: expand the plane waves in spherical harmonics

Solving Maxwell's Equations for Boundary Conditions



Apply Maxwell BCs:

$$\begin{split} &(\vec{E}_i + \vec{E}_s - \vec{E}_1) \times \hat{e}_r = 0 \\ &(\vec{H}_i + \vec{H}_s - \vec{H}_1) \times \hat{e}_r = 0 \end{split}$$

To get 4 equations for the 4 unknown coefficients, a_n , b_n , c_n , d_n

Mie Theory and Frohlich Condition

 For small particles using power series expansions of the j and h(1) functions to explicitly write out the first couple terms

$$a_{1} = -\frac{i2x^{3}}{3} \frac{m^{2} - 1}{m^{2} + 2} - \frac{i2x^{5}}{5} \frac{(m^{2} - 2)(m^{2} - 1)}{(m^{2} + 2)^{2}} + O(x^{6})$$

$$b_{1} = -\frac{ix^{5}}{45} (m^{2} - 1) + O(x^{7})$$

$$a_{2} = -\frac{ix^{5}}{15} \frac{m^{2} - 1}{2m^{2} + 3} + O(x^{7})$$

$$b_{2} = O(x^{7})$$

• The x dependance, for sufficiently small spheres a_1 is large to the exclusion of all other modes. Since the corresponding vector spherical harmonic is the Fröhlich (dipole) mode. The denominator of a_n vanishes (therefore infinite scattering) for:

$$m^2 = -\frac{n+1}{n} = -2$$

Mie Theory and Frohlich Condition

Frohlich mode n=1

$$m^2 = -\frac{n+1}{n} = -2$$

- To give $\varepsilon = -2\varepsilon_m$
- For Drude metal, using ε to find the Fröhlich mode frequency:

$$\omega_f = \frac{\omega_p}{\sqrt{1 + 2\varepsilon_m}}$$

Mie Theory and Frohlich Condition

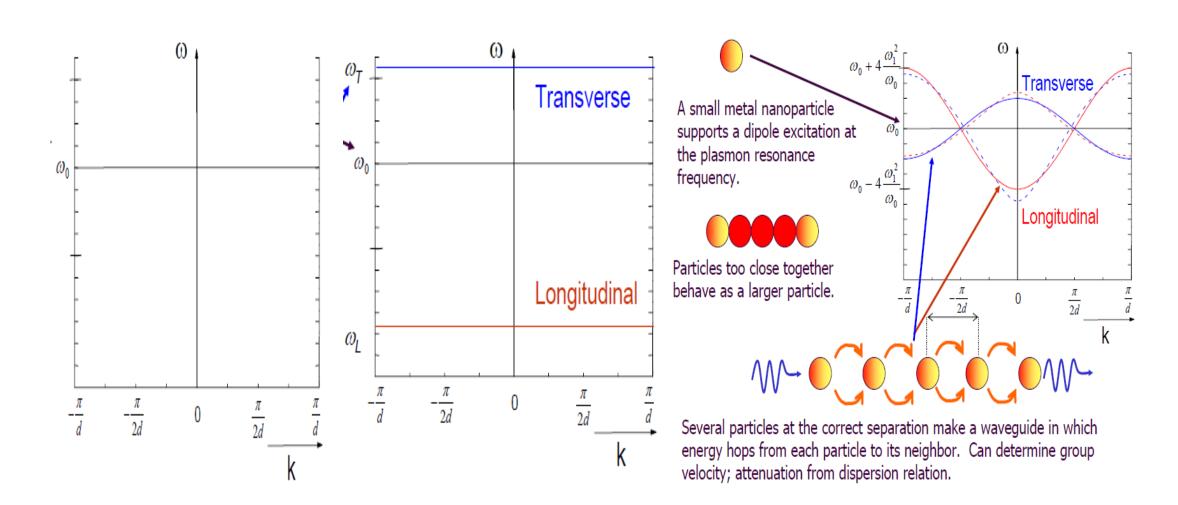
- At optical frequencies, a spherical metal nanoparticle can be represented as a dipole. Large scattering coefficient or plasmon resonance occurs near the virtual pole of the dipole normal mode.
- This peak occurs in visible wavelength for Ag, Au, Cu spheres in air.
- This quasistatic approximation agrees with measurements done on nanoparticles in different media.

Plasmonic waveguide

- Large number of these spherical nanoparticles kept far apart act as isolated dipoles supporting same plasmon resonance frequency.
- Large number of spherical nanoparticles kept too close together act as a larger elliptical particle giving two modes corresponding to the major and minor axis of the ellipse.
- When spaced at optimal distance they form a waveguide in which energy hops from each particle to its neighbour whose group velocity can be determined from dispersion relation.
- Mode splitting occurs because in longitudinal mode restoring force is reduced by coupling to shift resonance to lower frequency while in transverse mode restoring force is increased by coupling to shift resonance to higher frequency.
- Plasmons confined in metal nanoparticles have discrete resonant modes. Energy hops to neighbouring dipole in near fields.



Splitting of transverse and longitudinal modes



Metamaterials

- Metamaterials are artificially engineered materials specifically to have properties not found in natural materials.
- Properties such as negative refractive index which has both negative dielectric permittivity and magnetic permeability, negative refraction and inverse Doppler shift.
- Properties arise from structure rather than composition.

Metamaterials

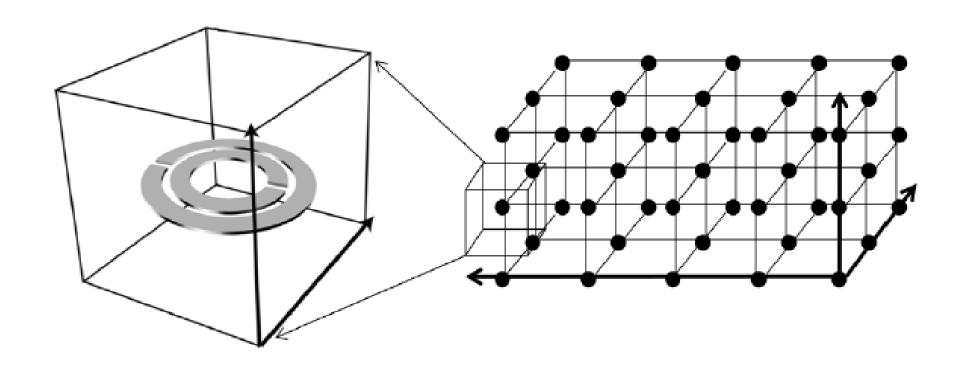
- Structural unit cell gives rise to specific properties which can be tuned.
- These unit cells are arranged in periodic structures with lattice parameters lesser than the wavelength of light so that they interact with light as an effective macroscopic medium.
- Effective parameters given by the relation

$$\varepsilon_{\text{eff}} \equiv \frac{\langle \mathbf{D} \rangle}{\varepsilon_0 \langle \mathbf{E} \rangle} \text{ and } \mu_{\text{eff}} \equiv \frac{\langle \mathbf{B} \rangle}{\mu_0 \langle \mathbf{H} \rangle}$$

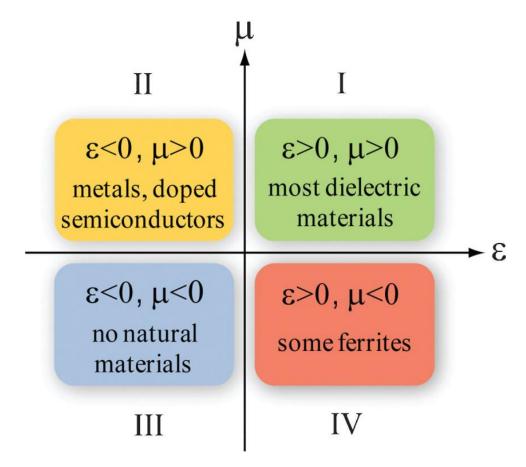
 Where D, E, B and H are the displacement field, electric field, magnetic flux density, and associated magnetic field, respectively. The symbol < > denotes a spatial average of the fields over the unit cell.

Metamaterial Lattice

 Individual unit composed of metal and dielectric materials with dimensions smaller than the wavelength of interest.



Negative Refraction



Negative Refraction

- In 1968 Veselago [7] proposed a theoretical material with simultaneous negative electric permittivity ϵ and magnetic permeability μ to have a negative refractive index n.
- Veselago's idea remained obscure as no natural materials were found having these properties.
- Maxwell's equations in isotropic medium without any sources are:

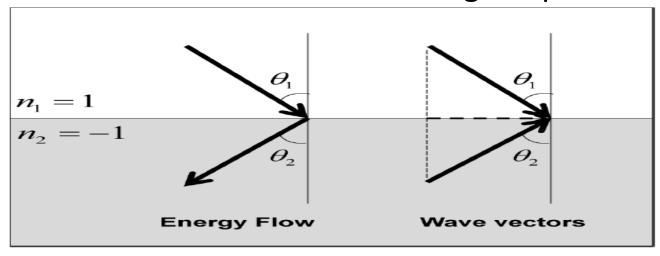
$$\mathbf{k} \times \mathbf{E} = \omega \mathbf{B} = \omega \mu_{\text{eff}} \mu_0 \mathbf{H} \text{ and } \mathbf{k} \times \mathbf{H} = -\omega \mathbf{D} = -\omega \varepsilon_{\text{eff}} \varepsilon_0 \mathbf{E}$$

Negative Refraction

- In the case of a double negative (DNG) medium, waves still can propagate through the medium but instead follow the left-handed rule $(E \times H = -k)$.
- Poynting vector is defined as S=E×H, the phase velocity (in the direction of k) is now opposite to the direction of group velocity (in the direction of S), indicating a backward propagating wave.

Light would then refract to the same side of the normal having antiparallel

phase and group velocity.



- One important characteristics of a negative index material is its ability to resolve beyond the diffraction limit.
- In 2000, it was proposed by Pendry that a slab of negative index material can overcome the resolution limit of conventional lenses to achieve a perfect lens [5].

• Imagine we have an infinitesimal dipole of frequency ω in front of a lens. Fourier expansion of electric field yields:

$$\mathbf{E}(\mathbf{r},t) = \sum_{\sigma,k_x,k_y} \mathbf{E}_{\sigma}(k_x,k_y) \exp(ik_z z + ik_x x + ik_y y - i\omega t)$$

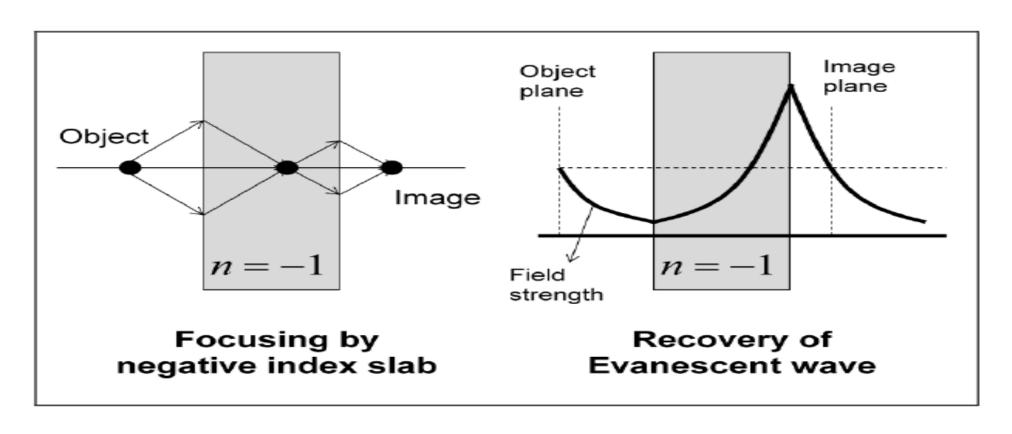
$$k_z = \sqrt{\omega^2 / c^2 - k_x^2 - k_y^2}$$

• For components satisfying $k_x^2+k_y^2>w^2/c^2$, kz becomes imaginary and therefore decaying exponentially with increasing z.

- Information of subwavelength features that are stored in higher inplane wavevectors will be lost as the observer goes far away from the object.
- Hence the resolution is determined from the maximum in-plane wavevector with real k_z , given by $\Delta = \frac{2\pi}{k_{max}} = \frac{2\pi c}{\omega}$
- However, if the medium has a negative index, the wavevector becomes opposite in sign, given by $k_Z'=-\sqrt{\frac{\omega^2}{c^2}-k_\chi^2-k_y^2}$, givning exponential growth of the evanescent field.

- This does not violate energy conservation because the evanescent field does not transport energy.
- A slab of negative index material can serve as a focusing lens due to negative refraction.
- This lens recovers not only propagating components, but also evanescent components by amplification of previously decaying components and therefore can recover information of features smaller than a wavelength.
- Ideally this lens does not have a resolution limit, and is called a perfect lens.

• In the optical regime, this concept was demonstrated using a silver slab lens by Fang et al. [6].



Advances in Negative Index Metamaterials

- Such negative index media (NIMs) were implemented at microwave frequencies by periodic assemblies of millimeter scale split ring resonators and wires [21, 22, 23].
- It was found that its scaling broke down at higher frequencies as the metal making the SRR starts deviating from ideal conductor behaviour.
- Three different groups independently found an alternating design using a pair of metal wires or plates separated by a dielectric spacer for magnetic resonance [24,25,26].

Advances in Negative Index Metamaterials

- To increase overlap, a 'double-fishnet' structure was used.
- A two dimensional negative refractive index material in blue-green visible region was demonstrated with ultrathin Au-Si3N4-Ag waveguide sustaining a surface plasmon polariton mode with antiparallel group and phase velocities [20].

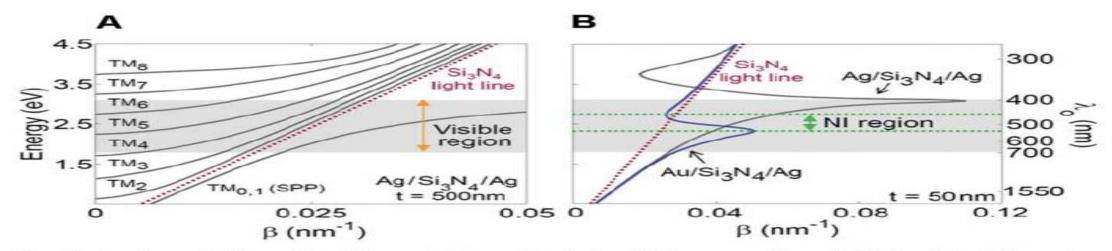


Fig. 1. Implementation of positive- and negative-index MIM waveguides. (A) Calculated dispersion curves for an $Ag-Si_3N_4-Ag$ waveguide with a dielectric core thickness t=500 nm. (B) Calculated dispersion curves for $Ag-Si_3N_4-Ag$ and $Au-Si_3N_4-Ag$ waveguides with t=50 nm.

- Optical modulators are usually composed of an active medium and an interferometer.
- The active medium's refractive index can be controlled by external stimulus.
- The index modulation in turn induces phase modulation of light that is interacting with the medium.

- The interferometer converts the phase modulation into the intensity modulation.
- An active medium is modulated most commonly by electro-optic effects or acousto-optic or a magneto-optic effect.
- The induced change in refractive index is very small, hence it requires either long interaction length in the device or a highly resonant cavity.

- Metamaterials offer control of the effective permittivity, permeability and therefore refractive index and impedance at certain frequency.
- An active metamaterial device operating at terahertz regime was demonstrated [15].
- The amount of the index change in the active medium is improved more than 16 times at telecommunication wavelengths with ultrafast response time of 1ps [27].

- At optical frequencies, fishnet metamaterial [28,29,24] is promising for an all-optical modulation.
- The anti-parallel current flow surrounding the dielectric medium induces a magnetic resonance, achieving negative permeability.
- By replacing the dielectric medium by photon sensitive semiconductors, such as Si or Ge, the effective index of the metamaterial can be modulated by the external optical pump.

• Equivalent circuit modeling of a magnetic resonator is done. In the case of split ring resonator (SRR), the effective permeability of the metamaterial composed of LC resonators can be described by

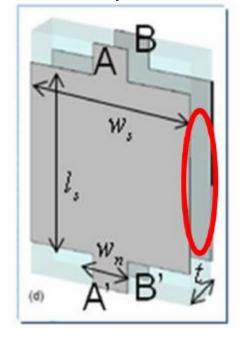
$$\mu_{eff}=1-rac{F\omega^2}{\omega^2-\omega_0^2+i\omega\Gamma}$$
 where $\omega_0=rac{1}{\sqrt{LC}}$

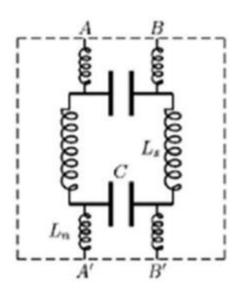
- Transmission and reflection through metamaterial slab can be modulated by applied electric field.
- In a fishnet metamaterial, at a certain wavelength near the resonance, the electric permittivity is negative due to the metallic wires parallel to the field direction and the magnetic permeability can be also negative due to the LC resonance of individual units.

Equivalent Curcuit Model for Metamaterial based Optical Modulators

• w and I are the width and length of wire, respectively, and t is the thickness of dielectric layer in the unit cell (n and s indicate thicker and thinner part of the unit cell)

$$C \sim \frac{lw}{t}, \frac{1}{L} \sim \frac{w_n}{l_n t} + \frac{w_s}{l_s t}$$





Fresnel Transmission and Reflection

 With effective parameters given, transmission and reflection coefficients of a metamaterial slab is calculated using Fresnel equation:

$$T = \frac{n_1}{n_3} \left| \frac{t_{12} t_{23} e^{ikd}}{1 + r_{12} r_{23} e^{2ikd}} \right|^2, \quad R = \left| \frac{r_{12} + r_{23} e^{2ikd}}{1 + r_{12} r_{23} e^{2ikd}} \right|^2$$

$$k_i = \sqrt{\varepsilon_i \mu_i (\omega/c)^2 - k_x^2}$$
, $r_{ij} = \frac{k_i / \mu_i - k_j / \mu_j}{k_i / \mu_i + k_j / \mu_j}$ and $t_{ij} = \frac{2k_i / \mu_i}{k_i / \mu_i + k_j / \mu_j}$

Fresnel Transmission and Reflection

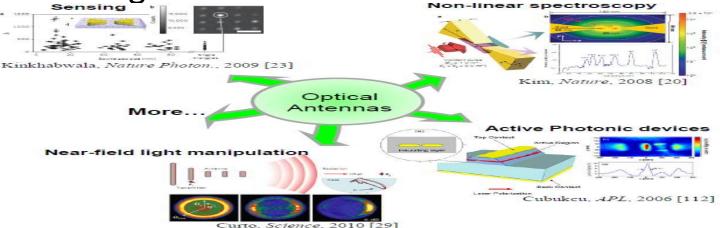
 After differentiation and using the fact that the thickness of metamaterial slab is very thin compared to the wavelength and the hosting medium is air, the modulation sensitivity equation for the transmission and reflection is:

$$\begin{split} \frac{dT}{d\varepsilon_d} \frac{1}{T} &= \frac{2A}{d} \left| \frac{\omega_0^2 (1-\mu_2)^2}{F\omega^2 C} \right| \frac{-2r(1-e^{2ikd})}{(1-r^2e^{2ikd})(1-r^2)} \left| \frac{\sqrt{\varepsilon_2}}{\sqrt{\mu_2} (\sqrt{\varepsilon_2} + \sqrt{\mu_2})^2} \right| \\ \frac{dR}{d\varepsilon_d} \frac{1}{R} &= \frac{2A}{d} \left| \frac{\omega_0^2 (1-\mu_2)^2}{F\omega^2 C} \right| \frac{(1+r^2e^{2ikd})}{r(1-r^2e^{2ikd})} \left| \frac{\sqrt{\varepsilon_2}}{\sqrt{\mu_2} (\sqrt{\varepsilon_2} + \sqrt{\mu_2})^2} \right| . \end{split}$$

• From the equations, the modulation is maximized when μ is near zero and the imaginary part of ϵ is maximized.

Optical Nanoantennas

- Plasmonic based Optical nano-antennas have been used for unique applications such as cloaking [30], higher harmonic generation [31], biological and chemical sensing [32-35], sub-diffraction lithography [36], optical imaging [37], energy harvesting [38].
- Field enhancement in sub-wavelength regions by optical nanoantennas is used in fluorescence and Raman spectroscopy with capabilities of single molecule sensing.



Summary

- Plasmonics and metamaterials being a rapidly growing field in research, there is a vast number of new fundamental phenomenon and its applications in technology that are exciting.
- Starting from the diffraction limit discovered by Abbe and Rayleigh, Kirchhoffs theory for diffraction from a small hole in metal sheet to Bethe's correction and finally the surprising experimental demonstration of enhancement of field by Ebbessen leading to consideration of plasmonics in the optical response of metals is discussed.

Summary

- Mie and Ritchie's study on scattering of light by spherical nanoparticles to realize localized surface plasmons are explained.
- Birth of new class of materials called metamaterials having novel optical properties and their demonstration by several groups led to possibility of subwavelength photonic devices.
- Some of the most important applications such as subwavelength imaging, plasmonic waveguides, perfect lens, Optical modulators and optical nanoantennas are described.

Summary

- There are several difficulties involved with fabrication of such materials which are being tackled by researchers.
- The possibility of optical devices replacing electronic devices can be realized much sooner than what we would have expected. There is still a huge amount of potential and applications to realize it are being searched for.

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